AN APPLICATION OF A FIXED-POINT THEOREM TO NEUMANN PROBLEMS ON THE SIERPINSKI FRACTAL

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Dedicated to prof. dr. Ioan A. Rus on the occasion of his 80th birthday.

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Abstract. We prepare first the background for the study of Neumann problems on the Sierpinski fractal in the N-dimensional Euclidean space. Hereafter we apply the Leray-Schauder continuation principle to prove the existence of at least one solution of certain Neumann problems on this fractal.
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