Fixed Point Theory, 19(2018), No. 2, 453-462
DOI: 10.24193/fpt-ro.2018.2.36
http://www.math.ubbcluj.ro/~nodeacj/sfptcj.html

LEFSCHETZ-TYPE FIXED POINT THEOREMS FOR SPHERIC MAPPINGS

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Dedicated to Professor Ioan A. Rus on the occasion of his 80th birthday

Abstract. Deterministic as well as random Lefschetz-type fixed point theorems are formulated for multivalued spheric maps on various sorts of special retracts in a Euclidean space.
Key Words and Phrases: Lefschetz theorem, fixed points, spheric mappings, random operators, retracts.
2010 Mathematics Subject Classification: 55M20, 47H10, 47H04, 47H40.

Acknowledgements. The first author was supported by the grant No. 14-06958S "Singularities and impulses in boundary value problems for nonlinear ordinary differential equations" of the Grant Agency of the Czech Republic.

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Received: June 7, 2016; Accepted: August 30, 2016.