

## RANDOM FIXED POINT THEOREMS FOR LOWER SEMICONTINUOUS CONDENSING RANDOM OPERATORS

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**Abstract.** In this paper, we study the existence of the random fixed points for lower semicontinuous condensing random operators defined on Banach spaces. Our results extend corresponding ones present in literature.

**Key Words and Phrases:** random fixed point theorem, lower semicontinuous operator, condensing operator.

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