

## ANSWER TO KIRK-SHAHZAD'S QUESTION ON ZHANG-JIANG'S FIXED POINT THEOREM

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**Abstract.** In this note we give a positive answer to Kirk-Shahzad's question on Zhang-Jiang's fixed point theorem [8, Question on page 18].

**Key Words and Phrases:** Partial order, Brézis-Browder order principle, fixed point.

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