

PROJECTIONS ONTO CONES IN BANACH SPACES

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Abstract. We propose to find algebraic characterizations of the metric projections onto closed, convex cones in reflexive, locally uniformly convex Banach spaces with locally uniformly convex dual.

Key Words and Phrases: Banach space, closed convex cone, metric projection.

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