

A CARISTI FIXED POINT THEOREM FOR COMPLETE QUASI-METRIC SPACES BY USING mw -DISTANCES

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Abstract. In this paper we give a quasi-metric version of Caristi's fixed point theorem by using mw -distances. Our theorem generalizes a recent result obtained by Karapinar and Romaguera in [7].

Key Words and Phrases: fixed point, w -distance, mw -distance, quasi-metric, complete quasi-metric space, Caristi's fixed point theorem.

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