FIXED POINT THEOREMS FOR COMPACT POTENTIAL OPERATORS IN HILBERT SPACES

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Abstract. The aim of this paper is to present new fixed point theorems for compact potential operators in Hilbert spaces. A variational approach is used and applications to boundary value problems illustrate the existence results.

Key Words and Phrases: Potential operator, critical points, fixed point theorem, boundary value problem.

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