*Fixed Point Theory*, 18(2017), No. 2, 445-456 DOI 10.24193/fpt-ro.2017.2.35 http://www.math.ubbcluj.ro/~nodeacj/sfptcj.html

# ON STABILITY AND HYPERSTABILITY OF AN EQUATION CHARACTERIZING MULTI-ADDITIVE MAPPINGS

## ANNA BAHYRYCZ

#### AGH University of Science and Technology, Faculty of Applied Mathematics Mickiewicza 30, 30-059 Kraków, Poland E-mail: bahyrycz@agh.edu.pl

**Abstract.** In this paper, using the fixed point approach, we prove some stability and hyperstability results for an equation characterizing multi-additive mappings. Our results generalize some known outcomes. In particular, we give a solution of a problem concerning optimality of some estimations. **Key Words and Phrases**: Multi-additive mapping, Hyers-Ulam stability, hyperstability, fixed point theorem.

2010 Mathematics Subject Classification: 39B52, 39B55, 47H10.

### References

- T. Aoki, On the stability of the linear transformation in Banach spaces, J. Math. Soc. Japan, 2(1950), 64–66.
- D.G. Bourgin, Approximately isometric and multiplicative transformations on continuous function rings, Duke Math. J., 16(1949), 385-397.
- [3] D.G. Bourgin, Classes of transformations and bordering transformations, Bull. Amer. Math. Soc., 57(1951), 223–237.
- [4] J. Brzdęk, Hyperstability of the Cauchy equation on restricted domains, Acta Math. Hungar., 141(2013), 58–67.
- J. Brzdęk, J. Chudziak, Zs. Páles, A fixed point approach to stability of functional equations, Nonlinear Anal., 74(2011), 6728–6732.
- [6] J. Brzdęk, K. Ciepliński, Hyperstability and superstability, Abstr. Appl. Anal., 2013(2013), Article ID 401756, 13 pp.
- [7] K. Ciepliński, Generalized stability of multi-additive mappings, Appl. Math. Lett., 23(2010), 1291–1294.
- [8] K. Ciepliński, Stability of multi-additive mappings in  $\beta$ -Banach spaces, Nonlinear Anal., **75**(2012), 4205–4212.
- P. Găvruţa, A generalization of the Hyers-Ulam-Rassias stability of approximately additive mappings, J. Math. Anal. Appl., 184(1994), 431–436.
- [10] D.H. Hyers, On the stability of the linear functional equation, Proc. Nat. Acad. Sci. U.S.A., 27(1941), 222–224.
- [11] M. Kuczma, An Introduction to the Theory of Functional Equations and Inequalities. Cauchy's Equation and Jensen's Inequality, Birkhäuser Verlag, Basel, 2009.
- [12] Gy. Maksa, Zs. Páles, Hyperstability of a class of linear functional equations, Acta Math. Acad. Paedag. Nyiregyháziensis, 17(2001), 107-112.

445

#### ANNA BAHYRYCZ

- W.-G. Park, J.-H. Bae, On the solution of a multi-additive functional equation and its stability, J. Appl. Math. Comput., 22(2006), 517–522.
- [14] W.-G. Park, J.-H. Bae, Solution of a vector variable bi-additive functional equation, Commun. Korean Math. Soc., 23(2008), 191–199.
- [15] W.-G. Park, J.-H. Bae, Stability of a bi-additive functional equation in Banach modules over a C\*-algebra, Discrete Dynam. Nat. Soc., 2012(2012), Article ID 835893, 12 pp.

Received: February 11, 2015; Accepted: October 30, 2015.

446