NEW RESULTS ON THE EXISTENCE
OF THE GENERALIZED PARETO EQUILIBRIUM

MONICA PATRICHE

University of Bucharest, Faculty of Mathematics and Computer Science
14 Academiei Street, Bucharest, Romania
E-mail: monica.patriche@yahoo.com

Abstract. In this paper, we state a new fixed point theorem for correspondences defined on Hausdorff locally convex spaces and we use it to prove the existence of the generalized weighted Nash equilibrium and the generalized Pareto equilibrium of a constrained multi-criteria game.
Key Words and Phrases: fixed point theorem, generalized weighted Nash equilibrium, generalized Pareto equilibrium, generalized multiobjective game.
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