

SELF-ADAPTIVE PROJECTION ALGORITHMS FOR SOLVING THE SPLIT EQUALITY PROBLEMS

QIAO-LI DONG* AND SONGNIAN HE**

*College of Science, Civil Aviation University of China
Tianjin 300300, China
E-mail: dongql@lsec.cc.ac.cn

**College of Science, Civil Aviation University of China
Tianjin 300300, China

Abstract. In this paper, we first introduce a self-adaptive projection algorithm by adopting Armijo-like searches to solve the split equality problem (SEP), then we propose a relaxed self-adaptive projection algorithm by using projections onto half-spaces instead of those onto the original convex sets, which is much more practical. Weak convergence results for both algorithms are analyzed.

Key Words and Phrases: Split equality problem, self-adaptive projection algorithm, relaxed self-adaptive projection algorithm, Armijo-like searches.

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