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N-ORDER UNIFORMLY NONCREASY BANACH LATTICES AND THE SUZUKI NONEXPANSIVE-TYPE MAPPINGS

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Abstract. We show that if K is a nonempty weakly compact convex subset of weakly orthogonal N-order uniformly noncreasy Banach lattice and $T : K \to K$ satisfies condition (C) or is continuous and satisfies condition (C_λ) for some $\lambda \in (0, 1)$, then T has a fixed point. This generalizes a result from [**?**].
Key Words and Phrases: Nonexpansive mapping, Fixed point, Weakly orthogonal lattice, Mapping satisfying condition (C_λ), N-order uniformly noncreasy Banach lattice.
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