APPLICATION OF A THREE CRITICAL POINTS THEOREM FOR A CLASS OF INCLUSION PROBLEMS

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Abstract. In this paper we prove the existence of at least three solutions for a differential inclusion problem involving the p-Laplacian with nonhomogeneous and nonsmooth Neumann boundary conditions. We use a three critical points theorem for locally Lipschitz functions given by A. Kristály, W. Marzantowicz, Cs. Varga [7].

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