CERTAIN FAMILIES OF ANALYTIC UNIVALENT FUNCTIONS GENERATED BY HARMONIC UNIVALENT MAPPINGS

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Abstract. In the present paper we obtain some inclusion theorems and convolution characterizations for the classes of analytic univalent functions generated by harmonic univalent and sense-preserving mappings.

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Key words. Harmonic mappings, univalent, sense-preserving, analytic, hypergeometric functions, subordination.

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