

ORBIT DECOMPOSITION OF SKEW GROUP ALGEBRAS

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**Abstract.** We describe the basic algebra Morita equivalent to the skew group algebra  $\Lambda G$ , where  $\Lambda$  is the path algebra of a finite, connected, acyclic quiver and  $G$  is a finite cyclic group. We give a structure theorem for the above case, based on combinatorial techniques. We prove that in this case  $\Lambda G$  is isomorphic to a direct product of certain matrix algebras, which are described in detail.

**MSC 2010.** 16G10, 16S35, 16W55.

**Key words.** Artinian rings, skew group algebras, basic algebra.

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