

International conference on MODULES AND REPRESENTATION THEORY Cluj-Napoca, July 7 – 12, 2008



## Vertices of simple modules for symmetric groups

Burkhard Külshammer

University of Jena [kuelshammer@uni-jena.de]

For a finite group G and a field F of characteristic p > 0, a vertex of an indecomposable module Mover the group algebra FG is a subgroup Q of G which is minimal with respect to the condition that M is isomorphic to a direct summand of  $\operatorname{Ind}_Q^G(\operatorname{Res}_Q^G(M))$ . The vertices of M form a conjugacy class of p-subgroups of G which are closely related to the defect groups of the block B of FG containing M. It is an open problem to determine the vertices of the simple FG-modules in the case where G is a finite symmetric group  $S_n$ . In my talk I will report on recent work of S. Danz, B. Fotsing, R. Zimmermann and myself.