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# ON $\tau$-COMPLEMENTED MODULES

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**Abstract.** For a hereditary torsion theory $\tau$, a module $A$ is called $\tau$-complemented if every submodule of $A$ is $\tau$-dense in a direct summand. We mainly study the class of $\tau$-complemented $\tau$-injective modules and its connections with some other classes of modules, such as the class of $\tau$-completely decomposable modules.

**MSC 2000.** 16S90, 16D70.

**Key words.** $\tau$-complemented module, $\tau$-completely decomposable module, $\tau$-injective hull.

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